

FAQs by Jack™ E

Tutorials about Remote Sensing Science and Geospatial Information Technologies

E: GRAND UNIFIED VEGETATION INDEX IMAGES

Like *Frequently Asked Questions*, a question is posed, e.g., [E1. Why Convert DNs to SRFIs?](#) Then, an answer is given¹ with comments and opinions. For cross referencing, each item is labeled, e.g., [E1](#).

This tutorial deals with [GRUVI.sml](#), its uses, and its options.

[GRUVI.sml](#) usually produces a **user-controlled pair** of **calibrated indicator rasters** called [GRUVI](#)² and [GRUBI](#).² Inputs to this script usually will be a **pair** of user-selected **SRFI** rasters (see [SRFI.sml](#) or [FAQs by Jack B.pdf](#)). However, [GRUVI.sml](#) may, instead, take, as input, a **pair** of **TC**² rasters, which also have **SRFI units** (see [TASCAP.sml](#) or [FAQs by Jack F.pdf](#)). In this case, the primary output raster is called [GRUFI](#)² instead of [GRUVI](#) as it is likely to not be an indicator of vegetation amount in the traditional sense of **Vegetation Indices (VIs)**. A small **Test Area** can optionally be used by the script to **optimize** the value of the **Background Noise Parameter**, **bnp**.

With appropriate control parameters, a [GRUVI](#) raster will be like one of the several classic **Vegetation Indices (VIs)**³: [NDVI](#), [Transformed NDVI](#), [SAVI](#), [TSAVI](#), or [WDVI](#). In many cases, the user will select [GRUVI](#) control parameters that produce **unique optimized** set of [GRUVI](#) and [GRUBI](#) rasters.

[GRUVI.sml](#) also may provide a solution to the **non-linear mixing problem** that faces the **MS** imagery analyst when dealing with **mixed vegetation and soil spectra**. Non-linear mixing occurs when foreground materials, e.g., vegetation, are partially transparent in one or more of the spectral bands that are involved as inputs to the [GRUVI](#) algorithm. In the usual application of [GRUVI.sml](#), the **near infrared (NR)** band (either **NA** or **NB**) is selected as the input **SRFIY** band (**Y-Axis**) and another band, e.g., **RL**, is selected as the input **SRFIX** band (**X-Axis**). Partial transparency creates a complex **non-linear spectral mixing** between **foreground vegetation** and **background materials** that have a range of brightness. The [GRUVI](#) algorithm is much like the [SAVI](#) algorithm (Huete, 1988); however, [GRUVI](#) is more flexible than the

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² [GRUVI](#) stands for **Grand Unified Vegetation Index**; [GRUBI](#) stands for **Grand Unified Brightness Index**. If the indicator raster is not vegetation related, then the output raster is called [GRUFI](#) instead of [GRUVI](#). Here, **F** is for **Foreground** materials. Examples would be **trees** or **water** as the subject "foreground."

³ Each **classic VI** acronym and formula is defined explicitly later in this tutorial. These usually well-known acronyms are referenced here for the sake of brevity.

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SAVI algorithm in that GRUVI can be optimized to minimize the disparate effects of variations in background brightness.

Input Data and Input Parameters for GRUVI.sml:

1. A pair of SRFI rasters or rasters having SRFI units (e.g., TC rasters). One input raster is likely to be either SRFINA or SRFINB; the other input raster then would be a visible-region or middle-infrared region raster, e.g., SRFIRL. The generic names of the input rasters are SRFIY and SRFIX, respectively.
2. The location of the Line of Background Materials (LBM) and the location of a Dense Vegetation (or Foreground Materials) Point in a SRFI 2-Space plot. The user provides this information in the form of five GRUVI control parameters: srfiX & srfiY for background materials, the slope of the LBM, and srfiX and srfiY for foreground materials (vegetation or possibly some other foreground materials).
3. A value for the GRUVI Background Noise Parameter (bnp).
4. An optional Test Raster set, called SRFIXT and SRFIYT. These may be used to optimize the value of bnp.

In addition, there are parameters hard-coded into the GRUVI.sml script that control the range of GRUVI, GRUFI, and GRUBI values and that designate the type of output rasters (16-bit or 8-bit as well as signed or unsigned). Nominally, GRUVI.sml produces 16-bit signed output rasters. GRUVI or GRUFI rasters have a numeric scale from 0 (for LBM materials) to 1000 (for vegetation or designated foreground materials). GRUBI rasters have a numeric scale equal to 20% of the related input SRFI units scale.

Since some pixels in a MS image have non-vegetation, non-foreground materials, and non-background materials as mixtures (or not), the output rasters, GRUVI or GRUFI and GRUBI, can (and will) have negative values. The use of signed integers allows all of the materials in a MS image to be represented by a continuum of numeric values. GRUVI.sml does limit the output numeric values to a range from -3000 to +3000. This also may be changed by changing the hard-coded value of grumax in the script.

If the user desires that the final rasters have only positive values, then the user should add an offset to each output raster value and assign the results of this post-processing operation to unsigned rasters. TNTmips, per se, handles signed rasters very well. However, if the rasters are to be provided to a non-TNTmips user, the output rasters may have to be further processed to create only positive values. There are many advantages for using TNTmips tools to handle rasters such as the outputs from GRUVI.sml.

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In Brief ...

This tutorial discusses key SML functions and model concepts related to **GRUVI.sml**. The list below is divided into two groups: one for the key **SML functions** and the other for **key model concepts**. If you are interested in a particular topic below, please go directly to it.

Sec.	Topic (Unique Topics are Bold)	Pages
	Quick Guide to GRUVI.sml	pp. E4-E7

KEY SML ITEM

There are no new SML functions in GRUVI.sml. Refer to SRFI.sml and DIAG.sml for information about the SUM functions that are in this script.

KEY MODEL-CONCEPT ITEMS

Sec.	Topic (Unique Topics are Bold)	Pages
E1.	Why Convert DNs to SRFIs?	pp. E8-E13
E2.	An Example of How GRUVI Compares to other VIs	pp. E14-E18
E3.	How GRUVI Optimizes the Structure of 2-Space	pp. E19-E25
E4.	Where Do I Get the GRUVI Control Parameters?	pp. E26-E29
E5.	Where Do I Get the GRUVI Test Rasters?	pp. E30-E30
E6.	Is There an Example of Non-Vegetation Indexing?	pp. E30
	REFERENCES	p. E31

Quick Guide to Using GRUVI.sml ...

If you are already familiar with SML functions and syntax ... and you just want to Run GRUVI.sml, this Quick Guide will help you.

BEFORE you use GRUVI.sml ...

- Run [SRFI.sml](#) to produce [SRFI](#), [PVI](#), and [PBI](#) rasters. These are used by [DIAG.sml](#) and [TERCOR.sml](#). If you plan to use both of these, run [TERCOR.sml](#) before you run [DIAG.sml](#).
- Select two rasters ([SRFI](#) rasters or [TC](#) rasters having [SRFI units](#)) to use as the two input rasters, called [SRFIX](#) and [SRFIY](#) in the [GRUVI](#) script. Most likely, this pair would be a [SRFIY](#) raster from one of the [near-infrared](#) bands ([SRFINA](#) or [SRFINB](#)) and a [SRFIX](#) raster from a [non-near-infrared](#) band ([SRFIRL](#), [SRFIGL](#), [SRFIMC](#), or [SRFIBL](#)). But, two [TC](#) rasters will also do.
- You probably need to have used [DIAG.sml](#) to produce [D](#) rasters for the same two selected bands, e.g., [DNA](#) and [DRL](#). Estimating the [five GRUVI control parameters](#) may be easier with [D](#) rasters than with other rasters. These five parameters are related to:
 - The [2-Space Point](#) on the [Line of Background Materials \(LBM\)](#)
 - The [Slope](#) of the [LBM](#) in [2-Space](#)
 - The [2-Space Point](#) representing vegetation or some other kind of foreground materials
- If you plan to optimize the output of [GRUVI.sml](#), you must extract a small [Test Raster set](#), called [SRFIXT](#) and [SRFIYT](#), from the selected [SRFIX](#) and [SRFIY](#) rasters before you run [GRUVI.sml](#). [GRUVI.sml](#) uses [SRFIXT](#) and [SRFIYT](#) to find the optimal value of the [Background Noise Parameter](#), [bnp](#), i.e., the value of [bnp](#) that minimizes the coefficient of variation [within the Test Raster set](#).
- You can, of course, choose to run [GRUVI.sml](#) with nominal control parameters and without the [bnp](#) optimization routine; however, the results will not be optimal and will likely be like one of the classic [Vegetation Indices \(VIs\)](#) that may be available as [TNTmips](#) menu-driven options. [GRUVI.sml](#) does allow you to select a set of control parameters that produce some classic or transformed [VIs](#) that are not currently in the [TNTmips](#) menu selections.

On [Pages 5 and 6](#), you will find [GRUVI Workflow & Control Parameters Forms](#) that you can use to [prepare for running GRUVI.sml](#). The sample entries in this form apply only to [QuickBird MS SRFI data for Yuma, CO, collected on July 2, 2003](#). These are not default or generic values that you may use for any scene.

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GRUVI Workflow & Control Parameters Form

Use with **REPAIR_RASTER.sml**, **SRFI.sml**, **DIAG.sml**, **TERCOR.sml**, and **GRUVI.sml**.

SAMPLE FORM: Completion Date: 04/26/05

INFO ITEM:	Value	INFO ITEM:	Value	INFO ITEM:	Value
Site Name:	Yuma, CO	Date Code:	20030702	Sun Elevation Angle (deg):	65.34
Imager Name:	QuickBird	Imager Number:	1	Correction Level:	3
hep:	80	msfac:	1.000	icRL:	1.34
Processing Date:	N/A	Product Source Code:	N/A	Gain Code:	N/A
Soil Search PVI Width:	100	Soil Search PBI Max:	1100	Veg Search PVI Min:	1300
Pure Soil Pixel SD Max:	14	Pure Veg Pixel SD Max:	23	Pure Pixel Box Size:	5
Skylight Fraction for GL Band fGL:	0.40	Sun Azimuth Angle (deg):	128.0	Viewing Angle: Off-Nadir Angle (deg):	25.0
Target Azimuth Angle (deg):	207.0	SRFIX Raster:	SRFIRL	SRFIY Raster:	SRFINA
Transformation Option:	Yes	Foreground Materials Point Xf:	305	Foreground Materials Point Yf:	3551
Line of Background Materials Slope:	1.0387	Background Materials Point Xb:	1681	Background Materials Point Yb:	2080
Extracted Test Area Available:	Yes	Background Noise Parameter bnp:	0.96	Analyst's Name:	Jack Paris
Comments:	In this case, GRUVI was customized to minimize the effects of wet soil due to irrigation in the agricultural fields.				

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GRUVI Workflow & Control Parameters Form

Use with **REPAIR_RASTER.sml**, **SRFI.sml**, **DIAG.sml**, **TERCOR.sml**, and **GRUVI.sml**.

BLANK FORM: Completion Date:

INFO ITEM:	Value	INFO ITEM:	Value	INFO ITEM:	Value
Site Name:		Date Code:		Sun Elevation Angle (deg):	
Imager Name:		Imager Number:		Correction Level:	
hep:		msfac:		icRL:	
Processing Date:		Product Source Code:		Gain Code:	
Soil Search PVI Width:		Soil Search PBI Max:		Veg Search PVI Min:	
Pure Soil Pixel SD Max:		Pure Veg Pixel SD Max:		Pure Pixel Box Size:	
Skylight Fraction for GL Band fGL:		Sun Azimuth Angle (deg):		Viewing Angle: Off-Nadir Angle (deg):	
Target Azimuth Angle (deg):		SRFIX Raster:		SRFIY Raster:	
Transformation Option:		Foreground Materials Point Xv:		Foreground Materials Point Yv:	
Line of Background Materials Slope:		Background Materials Point Xb:		Background Materials Point Yb:	
Extracted Test Area Available:		Background Noise Parameter bnp:		Analyst's Name:	
Comments:					

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As you run the script, the script will ask you to provide or to accept specific information items via a series of **Popup Windows**, in the following order:

- ❑ **CONSOLE-WINDOW ADJUSTMENT:** Use your mouse to adjust the size and placement of the **Console Window**. You need to be able to view its contents as the script runs and prints data to it.
- ❑ **SRFI TRANSFORMATION OPTION:** If you want to produce a **Classic VI**, answer **No**. Otherwise, answer **Yes**. But, if you answer Yes, you need to have already analyzed the input data to determine key biophysical parameters (listed below and in the **GRUVI FORM** above). The rest of the items here (below) assume that you have answered **Yes** to this question.
- ❑ **DENSE VEGETATION POINT: Xv or Xf:** Input the **value associated with dense vegetation** (or **foreground materials**) for the “X” raster. This comes from **your analysis of the data** in a **2-Space Raster Correlation** plot.
- ❑ **DENSE VEGETATION POINT: Yv or Yf:** Input the **value associated with dense vegetation** (or **foreground materials**) for the “Y” raster. This comes from **your analysis of the data** in a **2-Space Raster Correlation** plot.
- ❑ **LINE OF BACKGROUND MATERIALS SLOPE: slope:** Input the **slope associated with the Line of Background Materials**. This comes from **your analysis of the data** in a **2-Space Raster Correlation** plot where you used the **Equation Line**.
- ❑ **BACKGROUND MATERIALS POINT: Xb:** Input the **value associated with background materials** for the “X” raster. This comes from **your analysis of the data** in a **2-Space Raster Correlation** plot.
- ❑ **BACKGROUND MATERIALS POINT: Yb:** Input the **SRFI value associated with background materials** for the “Y” raster. This comes from **your analysis of the data** in a **2-Space Raster Correlation** plot.
- ❑ **BACKGROUND NOISE PARAMETER (bnp) OPTIMIZATION OPTION:** If you have extracted a small test area for this purpose, answer **Yes**. Otherwise, answer **No**.
- ❑ **BACKGROUND NOISE PARAMETER (bnp) ENTRY:** Either **accept** the **default bnp** value (from the last step). Or, **override** the default with your own **bnp** value, e.g., **1.0**.
- ❑ **SRFIX and SRFIY RASTERS** are **full-sized input rasters** (not test rasters).
- ❑ **GRUVI and GRUBI RASTERS** are **full-sized output rasters**. Put them in a **new Project File** (.rvc File).
- ❑ **The program runs to completion. Make a note of the type of GRUVI raster set produced in the COMMENTS in the GRUVI FORM.**
- ❑ **You may want to use the Right-Button option called Save as... to save the contents of the Console Window to a txt file.**

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E1. Why Convert DN's to SRFIs?

Almost without exception, every [Classic Vegetation Index \(VI\)](#) algorithm is based on a [pair](#) of selected [MS](#) image rasters. In most cases, this [pair](#) is a [near-infrared \(NR\)](#) band image ([NA](#) or [NB](#)) and a [visible-band](#) image ([RL](#) or [GL](#)). If available, the second image may be one of the [middle-infrared](#) bands ([MB](#), [MC](#), ..., [MG](#)). Most [VI](#) algorithms operate in a [2-Space](#) context (see [A19](#) and [A20](#) for details about [2-Space](#) and transformations from one [2-Space](#) context to another [2-Space](#) context).

If you want [VI](#) data to be [consistent from one date to another date and/or from one imager to another imager](#), the algorithms [must use calibrated reflectance-factor based estimates](#). [SRFI.sml](#) produces [calibrated SRFI](#) data. [SRFI](#) data can be improved by [TERCOR.sml](#) or [TASCAP.sml](#). Since the outputs from these scripts are rasters that have [SRFI](#) units, you can use them as inputs to [GRUVI.sml](#). In fact, if the terrain is not level, you should also run [TERCOR.sml](#) before using [GRUVI.sml](#). In most cases, you would also use [DIAG.sml](#) to produce [D](#) rasters that you can use to extract key parameters that [GRUVI.sml](#) needs as the basis for [2-Space Translation \(T\)](#) and [Rotation \(R\) transformations](#) (see [A20](#)).

Warning: If you apply [VI](#) algorithms to [uncalibrated DN's](#), e.g., [NA vs. RL](#), the resulting numeric values will also be [uncalibrated](#). This is a fact that seems to be poorly understood in the remote-sensing *user* community. Every software package has one or more [VI](#) tools that users can apply to [uncalibrated DN's](#) that they get from image-data providers. But, a [VI](#) algorithm is [not a magic, mystical process that somehow allows you to skip the data calibration step](#). [SRFI.sml](#) and its associated scripts are available to you to use [before](#) you apply any [VI](#) algorithm, [GRUVI](#) included, to the resulting [SRFI](#) rasters.

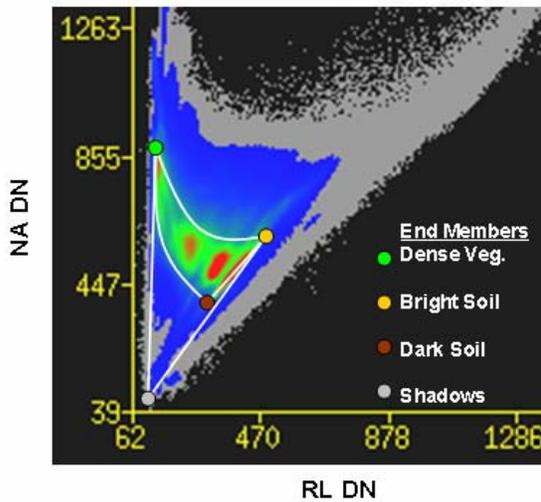
Consider a [2-Space](#) plot that involves the [uncalibrated DN's](#) from a [NA](#) raster versus the DN's from a [RL](#) raster. The sample data set for this consideration is a portion of [QuickBird MS](#) scene that was collected over [Yuma, CO](#), on [July 2, 2003](#). This data set is the same one used for illustrations about [SRFI.sml](#) (see [B](#)).

This sample set is used extensively throughout this tutorial.

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Figure E1A. 2-Space Plot of NA DN vs. RL DN for a QuickBird MS Image of Yuma, CO, July 2, 2003.



The four colored circles indicate the locations of pure spectral end members. Dense Vegetation is the green circle; Bright Soil, the yellow circle; Dark Soil, brown circle; and Shadows, the gray circle. The curved triangle, outlined by white lines, is called the Tasseled Cap (TC). White lines extend also from the TC area to the Shadow point. The overall area in the white lines shows where mixing among these four types of pure spectra can produce a mixed spectral property for a given pixel.

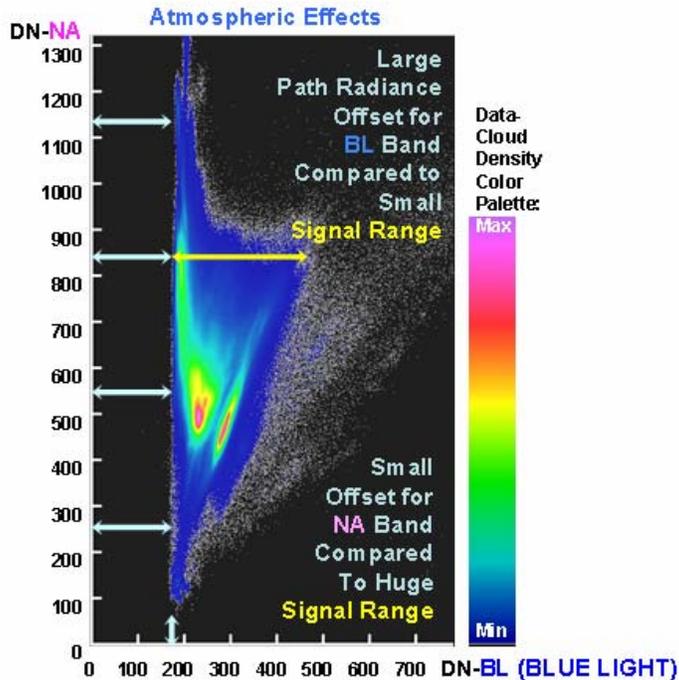
The line connecting the Dark Soil point to the Bright Soil point defines a Line of Background Materials (LBM) related to bare soils. Some Dense Vegetation pixels extend beyond the indicated Dense-Vegetation point to very high values of NA DN (while RL DN values remain low). Open water is very dark in the NA band and moderately dark in the RL band. Manmade materials tend to be very bright in both bands (tending toward the upper right).

Image pixels on the line between the Dark Soil point and the Bright Soil point are likely to be bare soil. Dense Vegetation pixels are likely to plot out near or above the Dense Vegetation point.

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[Figure E1B. 2-Space Plot of DN NA vs. DN BL for a QuickBird MS Image of Yuma, CO, July 2, 2003.](#)



This 2-Space plot is not exactly what you see when you use the **TNTmips Raster Correlation** tool. The author created this plot with a special **SML** script. Being zero based on both axes, this plot shows better the fact that **atmospheric reflectance (Path Radiance)** creates a **significant offset**, in the **BL** band. In this band, the **scene's Signal Range** is only about twice the **Path Radiance Offset** range. In addition, the scales of the two 2-Space axes are unequal.

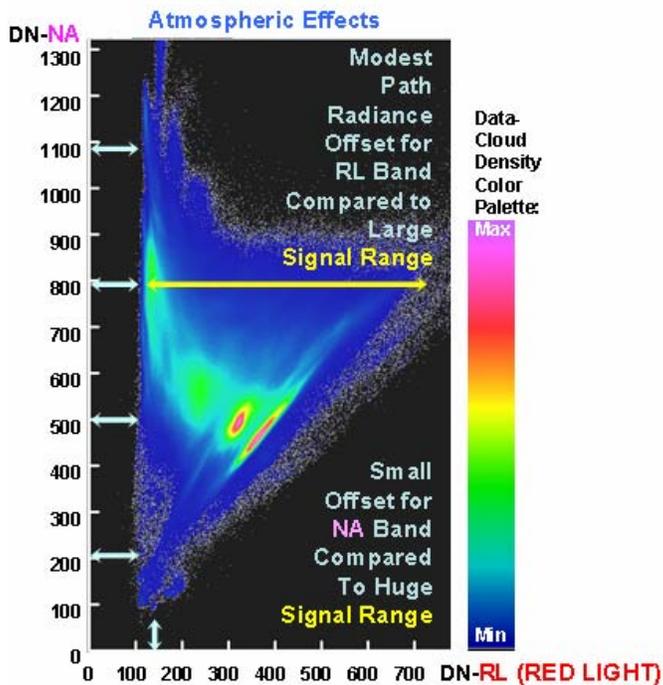
Thus, this 2-Space plot, which involves image **DNs**, is distorted and uncalibrated.

A similar situation exists for the 2-Space defined by **DN NA** vs. **DN RL** (see [Figure E1C](#) on the next page).

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Figure E1C. 2-Space Plot of DN NA vs. DN RL for a QuickBird MS Image of Yuma, CO, July 2, 2003.



The Path Radiance Offset (related to atmospheric reflectance) for the RL band is much smaller than the Signal Range. The highest density of data-cloud points are indicated by reddish colors. One feature that stands out is an elongated cluster of points related to bare soil pixels. This feature is close a line, called the Line of Background Materials (LBM), that is near the diagonal of the plot, i.e., where $DN_{NA} = DN_{RL}$. LBM has a slope of 1.25. If the NA scale were reduced, the slope might be 1.00. And, LBM might intersect at $DN_{NA} = 0$.

In the early history of Vegetation Index (VI) algorithm development, simple empirical equations were devised to combine DN_{RL} data and DN_{NA} data into a single numeric indicator (index) of the relative density of vegetation in each image pixel. The most famous empirical VI is the Normalized Difference Vegetation Index (NDVI). In terms of uncalibrated DN values,

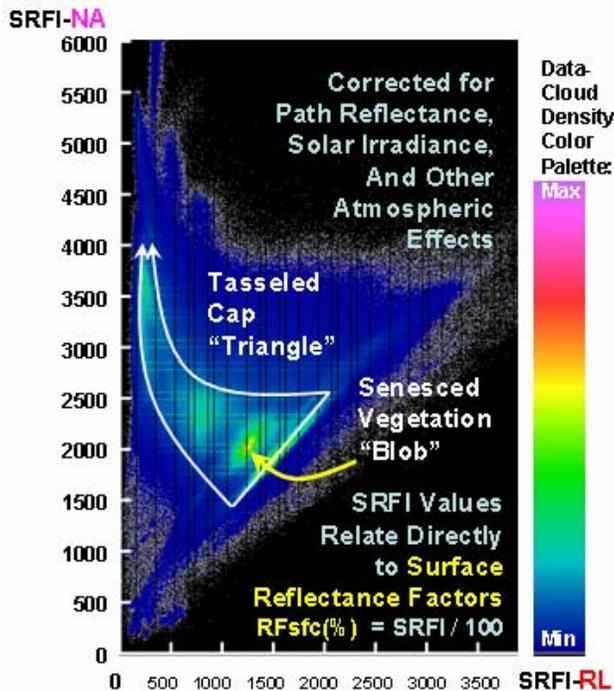
$$NDVI = (DN_{NA} - DN_{RL}) / (DN_{NA} + DN_{RL}) \quad (E1A)$$

Lines of constant NDVI (called isoveg lines) radiate the origin of the related 2-Space, i.e., from the point where DN_{NA} and DN_{RL} are both 0. Fortuitously, one of these isoveg lines runs close to LBM. In this case, the corresponding uncalibrated NDVI value is about 0.1111. At the tip of the Tasseled Cap distribution (see Figure E1A), the uncalibrated NDVI value is about 0.8000.

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Figure E1D. 2-Space Plot of SRFINA vs. SRFRL for a QuickBird MS Image of Yuma, CO, July 2, 2003.



Converting DNs to SRFI values adds value by:

- Correcting the data for atmospheric reflectance effects (path reflectance effects)
- Correcting the data for sun elevation angle effects, and
- Correcting the data for atmospheric transmission loss effects.

The Tasseled Cap feature is still present in this SRFI-related 2-Space plot.

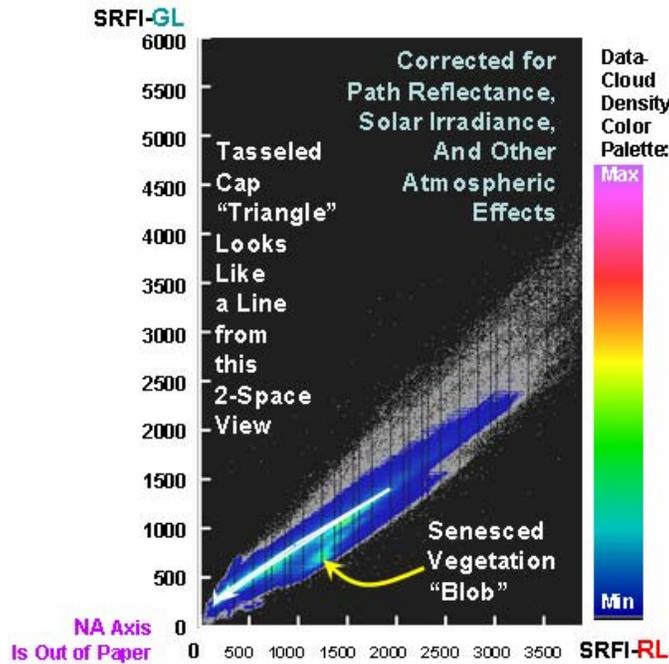
But, now the LBM and the Dense Vegetation Point have been moved to locations defined by calibrated SRFI values. The calibrated NDVI values, based on calibrated SRFI values, are now are 0.1076 for bare soil and 0.8471 the selected Dense Vegetation.

The use of a physically-based VI, such as the Soil Adjusted Vegetation Index (SAVI, see [A20](#)) or GRUVI, requires that the input data have calibrated reflectance-factor related units (like SRFI). Otherwise, the resulting VI values are unpredictable and have no physical relationship to biophysical variables in the vegetation being assessed.

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[Figure E1E. 2-Space Plot of SRFIGL vs. SRFRL for a QuickBird MS Image of Yuma, CO, July 2, 2003.](#)



This 2-Space plot of SRFIGL vs. SRFRL shows that the Tasseled Cap triangle appears to be a single line; however, this view is across the edge of the TC distribution. A benefit of this view is that a Senesced Vegetation "blob" is now seen as being a separate cluster that is not located within the domain of the TC triangle.

Thus, it is possible to construct a special GRUVI product that focuses on senescent vegetation in a way that is not confused by the presence of mixtures of emerged green vegetation and background soils of variable brightness.

E2. Is There an Example of GRUVI Compares to other VIs?

Consider the extracted image of an agricultural area near Yuma, CO, as shown in [Figure E2A](#).

[Figure E2A. Natural Color and Color IR Images of Yuma, CO, on July 2, 2003, Based on QuickBird MS.](#)

Natural Color vs. Color IR



Yuma, CO, July 2, 2003, Source: QuickBird MS Image

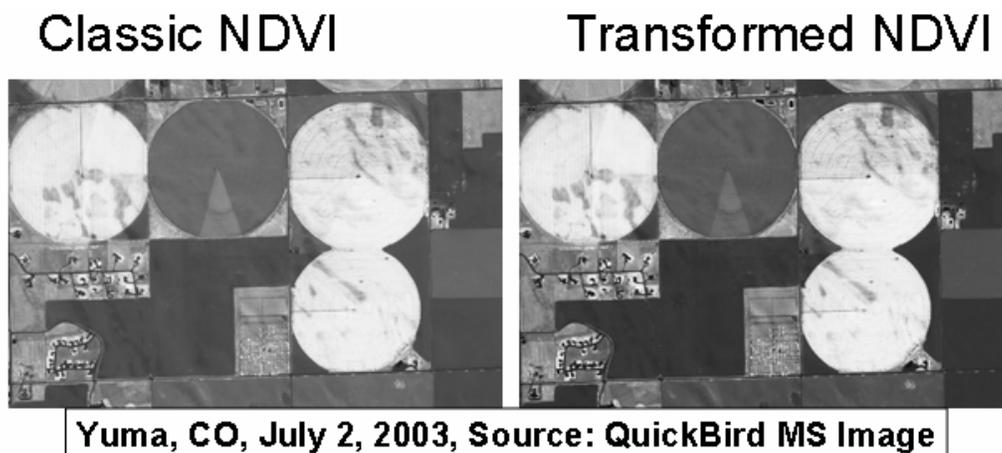
There are four center-pivot irrigated fields in this extracted scene. All of them are being affected by variations in surface soil brightness caused by the irrigation system. Wet plants also contribute to this effect. The effect of plant and soil wetness is most obvious in the south part of the top center circular field. The other three circular fields are corn fields near maximum biomass density. Variations in these fields are due to both wetness and biomass density. Some patches in these fields have poor soil, especially in the northern half of the upper right corn field. Residential areas, a cemetery, and other crops are also in this image (square and rectangular fields).

In general, it is difficult, if not impossible, to manually analyze these standard color images for the purpose of mapping out biomass density patterns in the presence of soil-wetness “noise.” [VIs](#) are designed to address this dilemma by providing a [single indicator of biomass density that is not affected by soil-brightness / wetness “noise.”](#)

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[Figure E2B. Classic NDVI and Transformed NDVI Maps of Yuma, CO, on July 2, 2003, Based on QuickBird MS.](#)

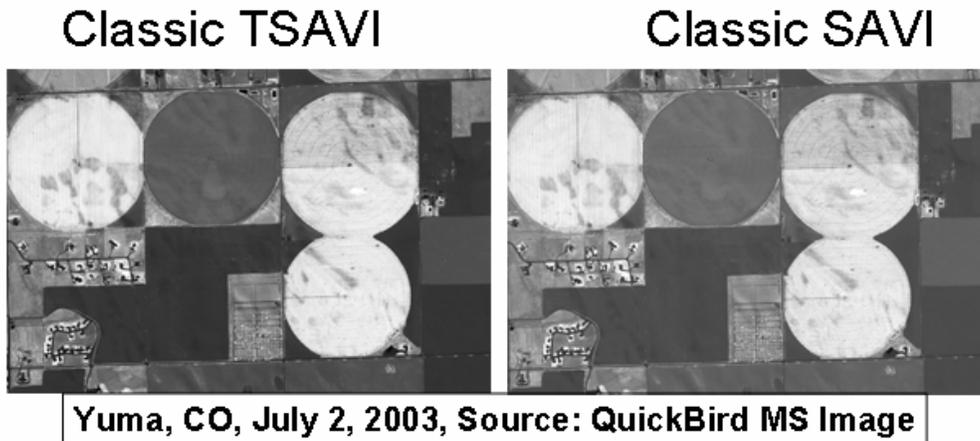


Classic NDVI is based on non-transformed values of SRFIRL and SRFINA. Thus, the Line of Background Materials (LBM) is not located on the line where SRFINA = SRFIRL. As a result, the SRFINA values are disproportionately higher than the SRFIRL values along the LBS. This causes the NDVI value to increase as the soil wetness (soil brightness) decreases. This is a significant noise effect that makes the wet part of the field appear to have a higher biomass density than it actually has.

An R and T transformation of the SRFINA and SRFIRL values moves the LBM to a position where Transformed SRFINA = Transformed SRFIRL. While this kind of transformation makes the Transformed NDVI have a zero (and constant) value for bare pixels, whether wet or dry, there still remains a significant effect of soil wetness in fields that are partly vegetated, e.g., the top center center-pivot field. The problem with the NDVI algorithm is that it produces isovegetation lines that are not parallel to the effects of soil wetness.

Huete (1988) addressed this basic defect in the NDVI algorithm by developing the Soil Adjusted Vegetation Index (SAVI). Baret (1989) modified SAVI to allow for the actual location of the LBM in a 2-Space plot of NR reflectance vs. RL reflectance. This modified version is called the Transformed SAVI (TSAVI). Other variations on SAVI and TSAVI are defined at the following Web site: <http://www.yale.edu/ceo/Documentation/rsvegfaq.html>

[Figure E2C. Classic TSAVI and Classic SAVI Maps of Yuma, CO, on July 2, 2003, Based on QuickBird MS.](#)



Both [TSAVI](#) and [SAVI](#) use formulas similar to [NDVI](#). [TSAVI](#) involves a coordinate stretch transformation of the [RL reflectance](#) axis *and* a translation shift of the [NR reflectance](#) axis. While this transformation moves the [LBM](#) to a desired diagonal position in the [transformed 2-Space](#), this kind of transformation [causes a scale change in the 2-Space](#).

[SAVI](#) uses a [SAVI soil noise parameter](#), L , which has a fixed value of [0.5](#). This is often too low for many cases. And, the axes of [NR](#) reflectance vs. [RL](#) reflectance are not transformed in the [SAVI](#) algorithm.

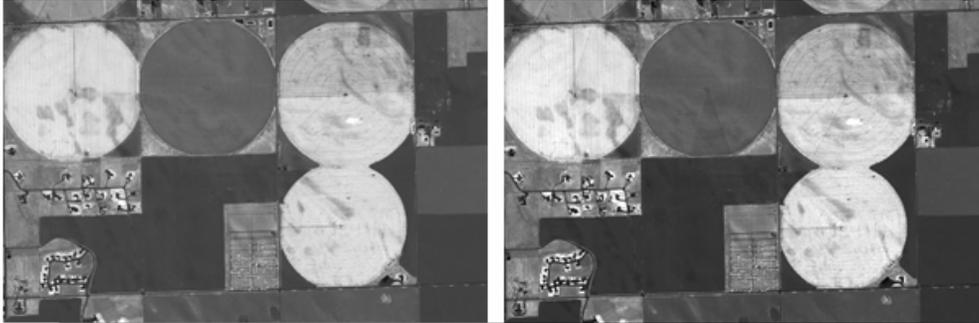
A way to view [SAVI](#) and [TSAVI](#) is that fixed displacement reflectance values are added equally to both the [NR](#) and [RL](#) reflectances before a [NDVI-like](#) formula is applied to the displaced (translated) data. The displacement is [0.25](#) (25% reflectance) for the [NR](#) data and [0.25](#) (25% reflectance) for the [RL](#) data. The total of these two displacements is equal to [0.5](#), which expressed as the [SAVI L](#) factor. In the case of [TSAVI](#), the displacement depends on the [LBS slope](#) and the [LBS NR intercept](#). A typical value of these [LBS](#) parameters leads to an effective value of $L = 0.15$. This is way too low for many cases.

A careful examination of [Figure E2C](#) shows that a small, but significant effect of soil wetness still exists in the top center pivot-irrigation field.

[Figure E2D. Optimized GRUVI and Weighted-Difference VI Maps of Yuma, CO, on July 2, 2003, Based on QuickBird MS.](#)

Optimized GRUVI

Weighted-Diff VI



Yuma, CO, July 2, 2003, Source: QuickBird MS Image

GRUVI addresses the flaws of NDVI, Transformed NDVI, SAVI, and TSAVI by first performing a [translation \(T\)](#) and [rotation \(R\)](#) transformation to SRFI values before applying a SAVI-type formula with a value of L that is optimized for the scene being analyzed. The T and R transformation preserves the SRFI scale of the input data (see [A20](#)); the RL scale expansion of all of the other classic transformed VIs does not preserve the scale of the input data. In addition, GRUVI determines the optimal value for its [background noise parameter, bnp](#), through a process of optimization using a test area in the image being analyzed. bnp plays a role similar to L in the SAVI algorithm. In the case of the map above, the optimized bnp value was 0.96 (as opposed to the value of L = 0.5 or = 0.15). If the slope of the LBS and its NR intercept change, bnp changes also.

The [Weighted Difference VI \(WDVI\)](#) is a [perpendicular-type VI](#). Effectively, if bnp is allow to take on a [very large value](#), e.g., 20.00, the [isovegetation lines](#) become parallel to the LBS – a primary main characteristic of all [perpendicular type VIs](#). Clearly, this value of bnp is not optimal. The effects of soil wetness are over-corrected in the WDVI image, i.e., the vegetation biomass density is underestimated.

The best of all of the VIs is the [Optimized GRUVI](#). A full-resolution, colorized map of [Optimized GRUVI](#) is shown on the next page in [Figure E2E](#).

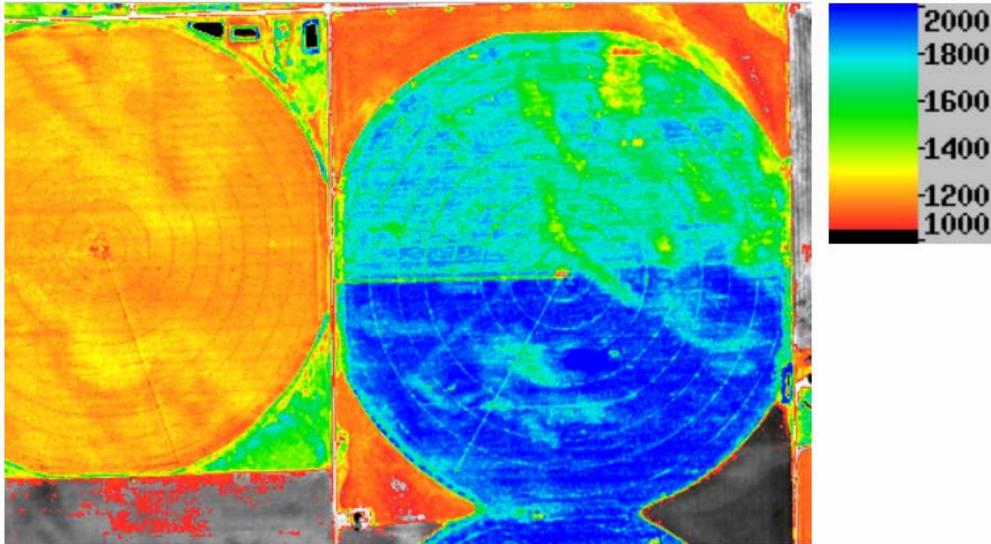
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[Figure E2E. Optimized GRUVI, with Color Scale Enhancement, for Yuma, CO, Based on QuickBird MS collected on July 2, 2003.](#)

Optimized GRUVI

Colorized to Improve Visibility of Biomass Variations over the Selected Field (North Half of Right Pivot)



This close-up and colorized map product shows that the effects of wet soil are completely removed by the [optimization process](#) available in the [GRUVI](#) algorithm.

In addition, the algorithm produces a [VI](#) map that has extended sensitivity to higher levels of biomass density. The top half of the right-hand pivot field is an R&D field that was receiving variable amounts of nitrogen applications. There are also poor soils in this half (due to iron chlorosis). The red patch in this field was a plot of corn that received no nitrogen application (as a control).

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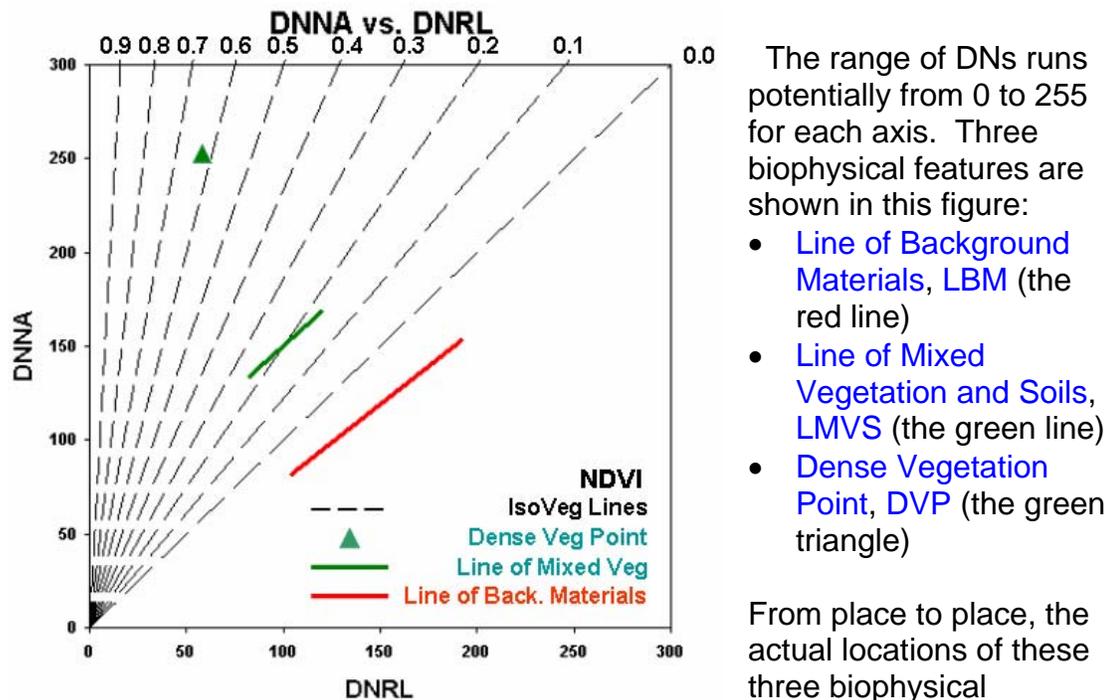
E3. How Does GRUVI Optimize the Structure of 2-Space?

While the maps above show that the [Translation \(T\)](#) and [Rotation \(R\)](#) operations associated with [GRUVI.sm1](#) seem to produce an optimized [Vegetation Index \(VI\)](#) map, it may still not be clear why this happens. This FAQ “answer” should make this clearer.

Let’s start with structure of the usual [2-Space](#) that involves the [NA](#) and [RL](#) bands (as [Y](#) and [X](#) data). This time, plots of 2-Space will be shown in a sequence from the original [DNs](#) to the final optimized transformed [SRFI](#) values.

Suppose that you have an image set consisting of 8-bit unsigned integers, e.g., from a Landsat 5 TM image. A plot of 2-Space might look like [Figure E3A](#):

[Figure E3A: Hypothetical NA vs. RL 2-Space for Image DNs.](#)



- The range of DNs runs potentially from 0 to 255 for each axis. Three biophysical features are shown in this figure:
- [Line of Background Materials, LBM](#) (the red line)
 - [Line of Mixed Vegetation and Soils, LMVS](#) (the green line)
 - [Dense Vegetation Point, DVP](#) (the green triangle)

From place to place, the actual locations of these three biophysical features ([LBM](#), [LMVS](#), and [DVP](#)) will change due to differences in soil type, degree of mixing between vegetation and soil, and type of vegetation. When [DNs](#) are used to define a [2-Space](#) plot, many other effects are involved including the gain of the sensor, the sun elevation angle, the atmospheric conditions, and terrain conditions.

An image [DN](#) is an arbitrary brightness scale that varies from one spectral band to another spectral band and that does not, without conversion to reflectance, relate to any physical property.

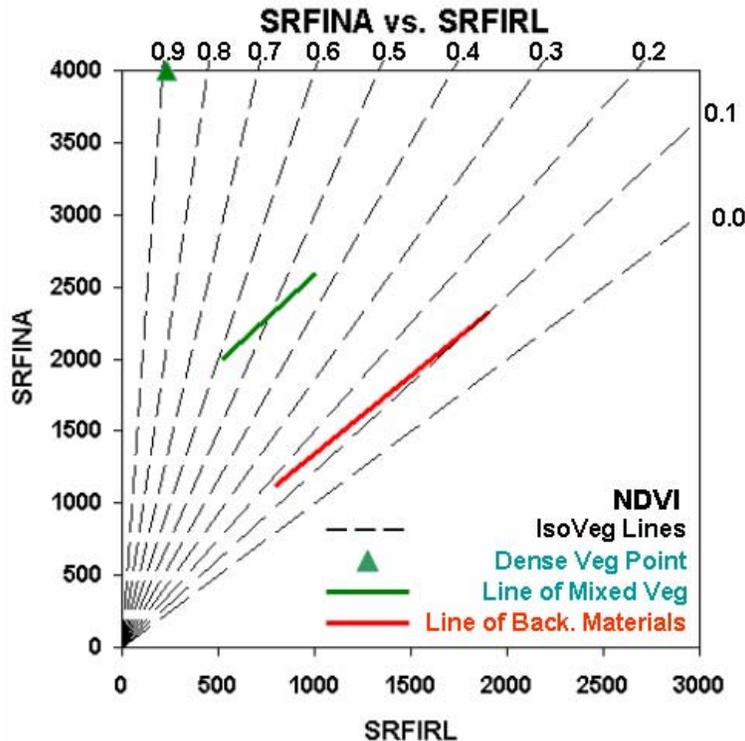
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Often, an analyst will apply the **NDVI** algorithm to **DNs** perhaps with the vague (and unfounded) hope that it somehow deals successfully with the uncalibrated nature of DN data.

The dashed lines show lines of constant **NDVI** values in this **uncalibrated 2-Space**. The value of **NDVI** along each dashed line is denoted at the upper end of each line by a number, such as 0.0, 0.1, ... or , 0.9. These **dashed lines** are called **isovegetation lines** since **NDVI** (an indicator of vegetation amount) is **constant (iso)** for all locations in **2-Space** on each **isovegetation / NDVI** line. Since it is common practice to use **only positive values of NDVI** for an output **NDVI** product raster, no isovegetation lines are shown for negative values of **NDVI**. Thus, all of the pixels that plot on or near the **LBM** (bare soil pixels and some sparsely-vegetated pixels above it) would have a **NDVI** value of **0.0** in an output raster. This explains why some analysts have said that they cannot detect small amounts of emergent vegetation in a **NDVI map** that is based on **uncalibrated DNs**. Vegetation has to “grow” for a while for it to reach the **isovegetation line associated with NDVI = 0.0**.

The difficulties associated with a **2-Space** plot based on **DNs** is somewhat resolved when the **DNs** are converted to **reflectance units**, e.g., to **SRFI values** (say with **SRFI.sml**).

Figure E3B: Hypothetical NA vs. RL 2-Space for SRFI Values.



In a **SRFI-based 2-Space** plot like this, all three biophysical features (**LBM**, **LMVS**, and **DVP**) are in the domain of positive values of **NDVI**. But, the **LBM** and the **LMVP** do not run parallel to the **NDVI** isovegetation lines. And, the location of the **LBM** is not near the isovegetation line where **NDVI = 0**.

It would make more sense to have a **VI** be equal to **zero** where no vegetation exists, i.e., along the **LBM**. And, it would be

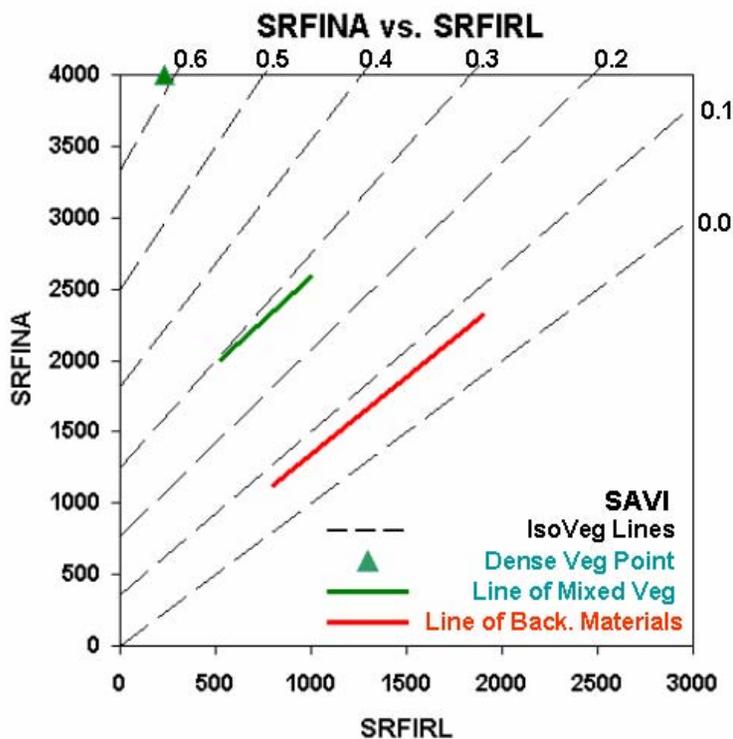
desirable that variations in the brightness of mixed vegetation and soils have a constant value for the associated **VI**. Therefore, it is obvious that **NDVI**,

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even based on **SRFI** values, still suffers from noise caused by variations in soil brightness (both for bare soil and for a mixture of foreground vegetation and background vegetation).

The **Classic SAVI** algorithm simply moves the **convergence point** of the isovegetation lines from (**SRFIRL = 0 and SRFINA = 0**) to **SRFIRL = -2500 and SRFINA = -2500**). This equal translation of the two **SRFI** axes is controlled by the **L** factor in the **SAVI** equation.

[Figure E3C: Hypothetical NA vs. RL 2-Space for SRFI Values with Isovegetation Lines Associated with the Classic SAVI Algorithm.](#)



This change has improved the alignment of the resulting SAVI isovegetation lines with the LBM and LMVS. But, the alignment is not perfect. And, the BLM is still located on an isovegetation line where SAVI is not equal to 0.

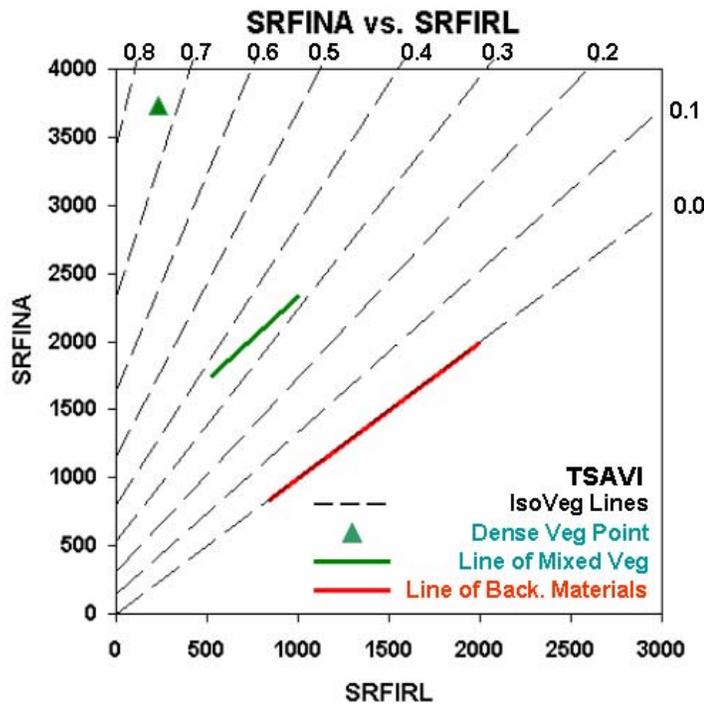
One way to fix the problem of **NDVI** values or **SAVI** values not being zero on the LBM is to transform the **SRFI** values by first performing a **Translation offset** equal to the **intercept of the**

LBM on the SRFINA axis and second by performing a **Rotation** that aligns the **VI = 0 isovegetation line** with the **LBM** (where bare-soil pixels are found).

[Figure E3D](#) (next page) shows the results of this **T and R** transformation for an algorithm called **TSAVI**. The **L** factor for **TSAVI** is only about **0.15** (rather than **0.5** as it was for **SAVI**).

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Figure E3D: Hypothetical NA vs. RL 2-Space for SRFI Values with Isovegetation Lines Associated with the Classic TSAVI Algorithm.



While the transformation associated with TSAVI fixed the alignment problem for the LBM, it did not fix the alignment problem for the LMVS.

The obvious problem lies with the location of the convergence point associated with Classic TSAVI, $SRFIRL = -750$ and $SRFINA = -750$. This convergence point is too close to (0,0) to flatten out the slopes of the isovegetation lines in this T & R transformed 2-Space.

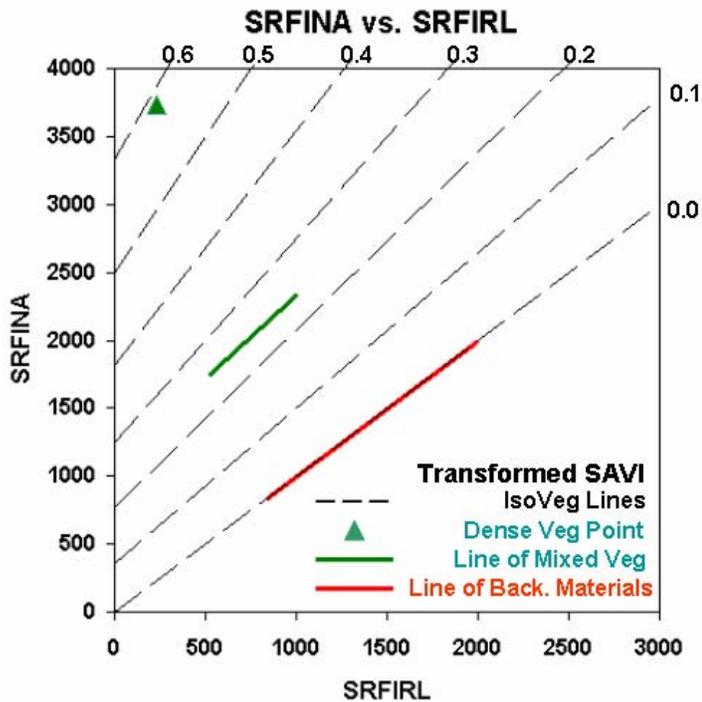
This suggests that SAVI's larger L-factor (0.5) might work better with the transformed SRFI axes. This idea is used for the Transformed SAVI data in [Figure E3E](#). Note that this Transformed SAVI is not the same as TSAVI.

The Transformed SAVI benefits from the fact that it includes a scale-preserving T & R transformation and the more optimum value for L, which is 0.5.

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Figure E3E: Hypothetical NA vs. RL 2-Space for SRFI Values with Isovegetation Lines Associated with a Transformed SAVI Algorithm.



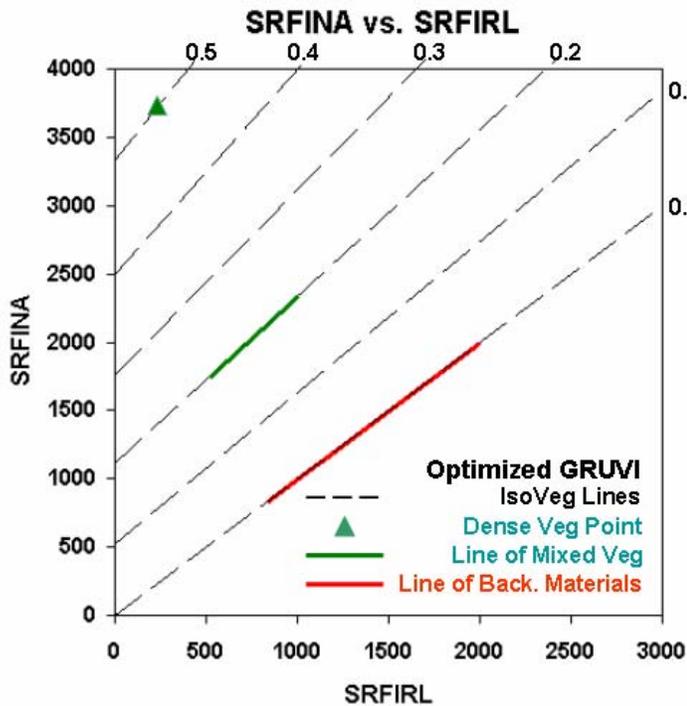
This non-classic SAVI is an improvement over all of the foregoing VIs. It puts the LBM on isovegetation line where Transformed SAVI = 0. And, it has a good alignment for the LMVS, better than TSAVI or Classic SAVI.

The isovegetation lines for this Transformed SAVI are the same as they are for the GRUVI algorithm with a Background Noise Parameter, bnp , of 0.5.

GRUVI.sml has a routine that optimizes the bnp based on a Test Area where the effect of background noise is very evident for a partly-vegetated field (like the green line in this 2-Space plot). For this hypothetical data set, the optimized value of bnp turns out to be 1.0. Figure E3F (next page) shows the results of using $bnp = 1.0$, rather than $bnp = 0.5$ (as in Figure E3E).

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[Figure E3F: Hypothetical NA vs. RL 2-Space for SRFI Values with Isovegetation Lines Associated with the Optimized GRUVI Algorithm.](#)



As indicated, both the **LBM** and the **LMVS** features are perfectly aligned with the isovegetation lines from the **Optimized GRUVI** (where $bnp = 1.0$).

The isovegetation lines here converge to a point where $SRFIRL = -5000$ and $SRFINA = -5000$. These negative offsets are each equal to minus $bnp * 5000$.

As bnp is allowed to increase to large values, say up to **20.0**, the isovegetation lines

become parallel to each other and to the **LBM**. This property is characteristic of the **Perpendicular Vegetation Index (PVI)** as shown in [Figure E3G](#) (next page).

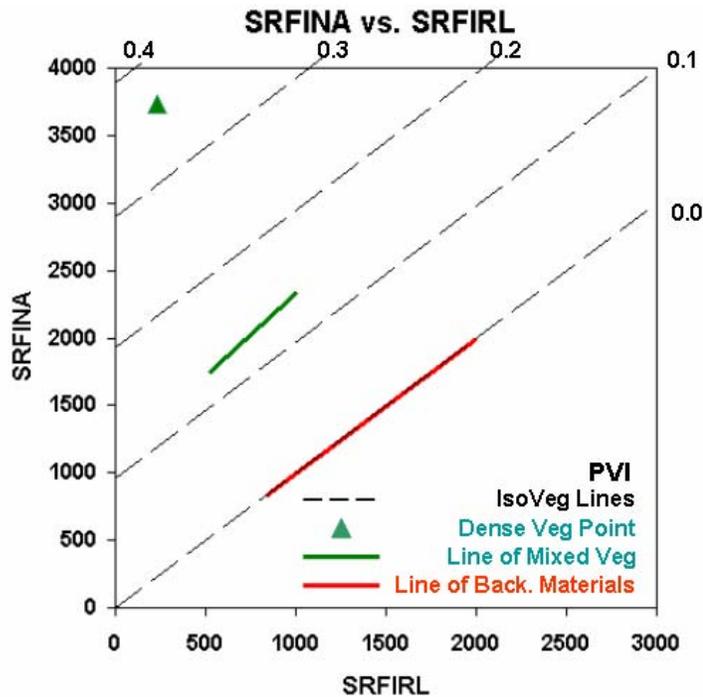
This initial floating-point value of the **Optimized GRUVI** is **rescaled** so that the **Dense Vegetation Point** has a final GRUVI value of **2000** and the **LBM** has a final GRUVI value of **1000**. With this rescaling, features that plot out **below** the **LBM** will have values of GRUVI between **0** and **1000**.

GRUVI.sml also produces a **GRUBI** raster that has a set of **GRUBI isobrightness** lines that are **perpendicular** to the **GRUVI isovegetation** lines.

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Figure E3G: Hypothetical NA vs. RL 2-Space for SRFI Values with Isovegetation Lines Associated with the PVI Algorithm.



Using `bnp = 20.0` (the value associated with `PVI`), the LMVS feature is again poorly aligned to the isovegetation lines.

`GRUVI.sml` contains a routine that optimizes the value of `bnp` for each scene based on a selected small Test Area where the effects of background brightness noise on `SRFIX` and `SRFIY` are evident (for a partly vegetated field).

Since calibration errors vary from scene to scene and since soil and vegetation structure varies from field to field, there is not a universal value for `bnp` that is optimal for all situations. `GRUVI.sml` addresses this reality by optimizing on the scene being analyzed.

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E4. How do I Get the GRUVI Control Parameters?

If you elect to [optimize](#) the GRUVI algorithm, you must provide five GRUVI control parameters: [srfiXb](#), [srfiYb](#), [slope](#), [srfiXv](#), and [srfiYv](#).

- [srfiXb](#) and [srfiYb](#): These are the [coordinates](#) of any selected point near the center of the [Line of Background Materials \(LBM\)](#) in the [2-Space](#) defined by a plot of [SRFIY vs. SRFIX](#).
- The [slope](#) of the [LBM](#) in the [2-Space](#) defined by a plot of [SRFIY vs. SRFIX](#).
- [srfiXb](#) and [srfiYb](#): These are the [coordinates](#) of a [cluster of dense vegetation](#) in the [2-Space](#) defined by a plot of [SRFIX vs. SRFIY](#).

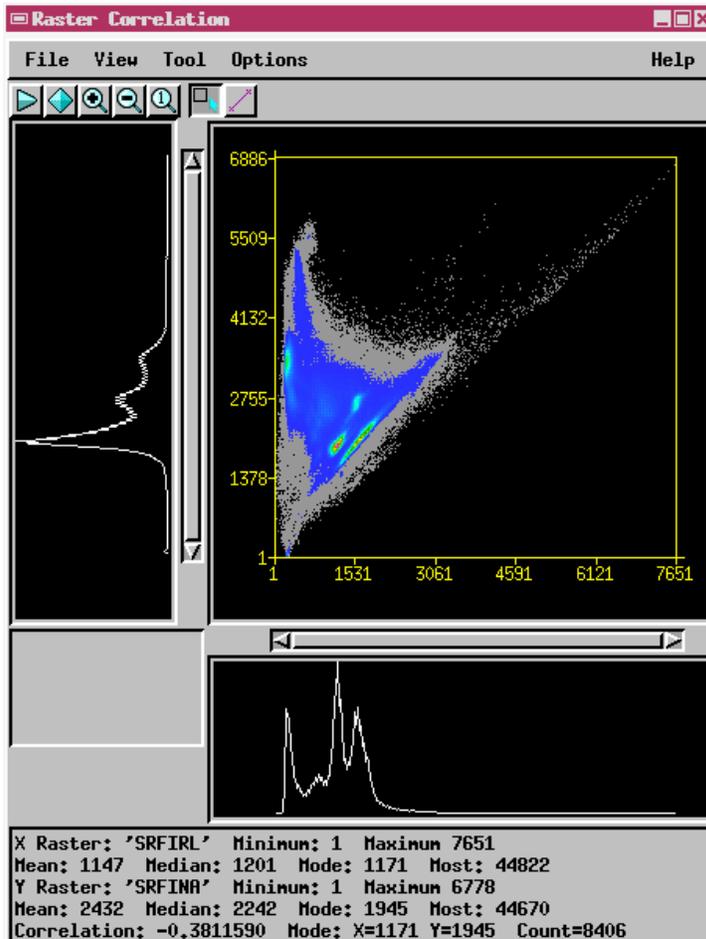
All five of these GRUVI control parameters can be estimated by using the [TNTmips Raster Correlation](#) tool. Here is the step-by-step procedure for using this tool for this purpose.

From the [TNTmips main menu](#):

- Follow the following menu path: [Display](#) > [Spatial Data...](#) > [New 2D Group](#). The [Group 1 – View 1](#) and [Group 1 – Group Controls](#) windows appear.
- Now [Add](#) (a new [Single](#)) [Raster](#) to [Group 1](#). This should be one of the two [SRFI](#) or [SRFI type](#) rasters that you will be in the GRUVI process. Suppose that this is the [SRFINA](#) raster from the [QuickBird](#) scene used above. It will appear in the [Group 1 – View 1](#) window as a grayscale image. An item will appear in the [Group 1 – Group Controls](#) window that is related to this single raster.
- Click on the [Tools](#) icon associated with the single raster item. Select the [Raster Correlation...](#) option. The [Raster Correlation](#) window opens with a blank (black) screen.
- Under the [File](#) menu, select [New](#). A [Select Objects](#) window opens. It needs for you to select a raster to assign to the [X Axis](#) and one to assign to the [Y Axis](#). Navigate to the TNTmips Project File (.rvc) that has the [SRFI](#) rasters for the scene being analyzed.
- Select an appropriate raster for the [X-Axis](#). For example, you can select the [SRFIRL](#) raster or the [SRFIGL](#) raster or the [SRFIMB](#) raster. This is the raster that is paired up with the [SRFINR](#) raster ([SRFINA](#) or [SRFINB](#)) to define the [SRFI-type 2-Space](#) being used as inputs to [GRUVI.sml](#).
- Select an appropriate raster for the [Y-Axis](#). For example, you can select [SRFINA](#) or [SRFINB](#). When this selection (when you click [OK](#)) is done, TNTmips produces a [2-Space plot](#) of the [Y](#) raster vs. the [X](#) raster, e.g., [SRFINA vs. SRFIRL](#). You may get a plot that looks like [Figure E3A](#) (next page). This is a color-coded data-cloud density plot (see [A19](#)) of the data in this defined [2-Space](#). The palette of colors used in this figure (and remaining figures) as associated with [TNTmips Version 7.1](#). [Prior versions of TNTmips](#) use a standard color palette that is less optimum (compared to [Version 7.1](#)) – but still is quite adequate.

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[Figure E3A. SRFINA vs. SRFIRL 2-Space Plot with Data-Cloud Density Shown by the Default Raster Correlation Color Palette \(as of TNTmips Version 7.1\).](#)



- The location of the elongated cluster (brown colors) related to the [Line of Background Materials \(LBM\)](#) associated with [bare soil](#) can be seen near the [brim](#) of the [Tasseled Cap](#) feature. If you click the [Zoom-In](#) icon, you will be able to see this [LBM](#) feature better (see [Figure E3B](#) on the next page).
- Move your mouse to the [center](#) of the [LBM](#) feature. The [X](#) and [Y](#) coordinates for this position will be displayed in the gray area of the plot (lower left). These are the values for the [srfiXb](#) and [srfiYb](#) parameters needed by [GRUVI](#) (when you run this script). In this case, [srfiXb = 1681](#) and [srfiYb = 2080](#).
- Now, move your mouse to the [center](#) of the [Dense Vegetation](#) feature (See [Figure E3C](#) on the next page). These are the values for the [srfiXv](#) and [srfiYv](#) parameters needed by [GRUVI](#) (when you run this script). In this case, [srfiXb = 305](#) and [srfiYb = 3551](#).
- To estimate the [slope](#) of the [LBM](#), turn on the [Equation Line](#) tool by clicking the right-most icon in the [Raster Correlation](#) tool above the [2-Space](#) plot. Use your mouse to draw a line in the [2-Space](#) plot area. Then, use the [handles](#) at the ends of this [Equation Line](#) to position it along the center of the elongated cluster of [LBM](#) points. This is shown in [Figure E3D](#) (on the next page).

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Figures E3B (left) and E3C (right). SRFINA vs. SRFIRL 2-Space Plot with Data-Cloud Density Shown by Raster-Correlation Standard Palette (Version 7.1) with Mouse Cursor Pointing to the Center of the Line of Background Materials (left) and to the Dense Vegetation Point (right).

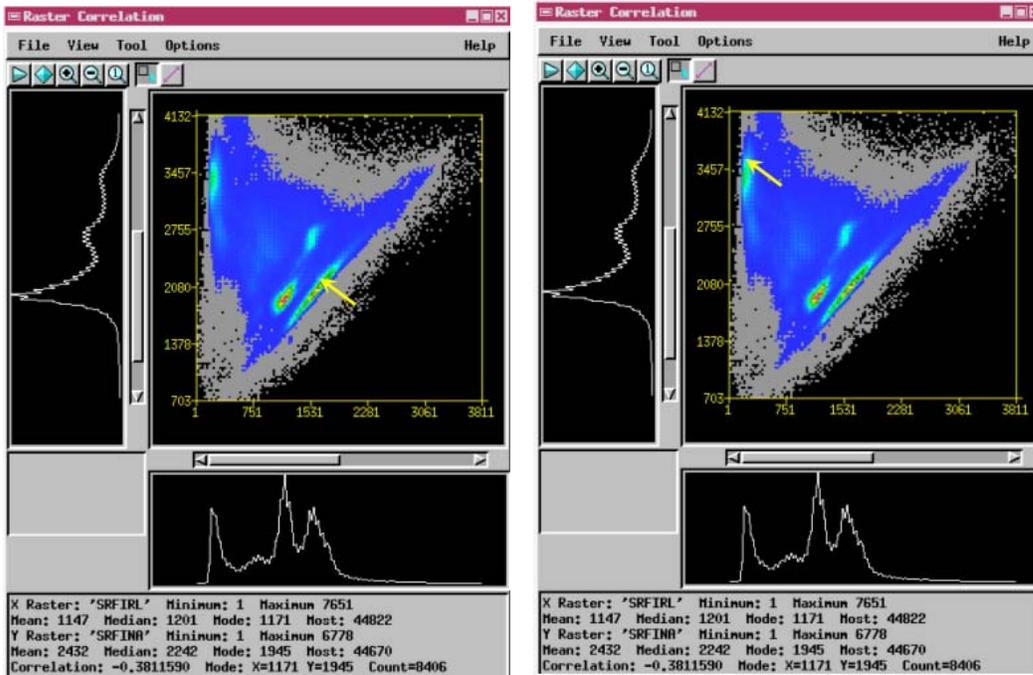
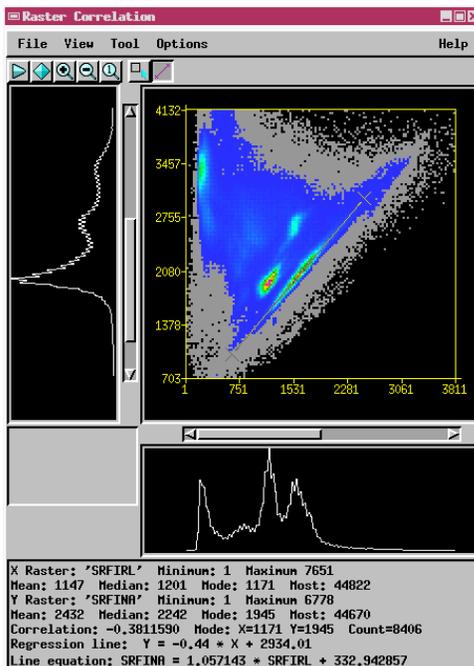


Figure E3D. Using the Equation Line Tool to Estimate the Slope of the LBM in the 2-Space Defined by SRFINA vs. SRFIRL.



The slope of the LBM is reported in the information below the plot as the Line equation: $SRFINA = 1.057143 * SRFIRL + 332.942057$. So, slope = 1.0571.

With these parameters, you are almost ready to run [GRUVI.sml](#).

See the next FAQ for the final preparation: [Extraction of a Test Raster](#) that [GRUVI.sml](#) will use for optimization of the [GRUVI bnp](#) control parameter.

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E4. Where do I get the GRUVI Test Rasters?

You use the [Raster Extract](#) tool to extract a small raster set that will be used by [GRUVI.sml](#) to optimize the [GRUVI bnp](#) control parameter.

Here is how you do this with [TNTmips](#).

From the [TNTmips main menu](#):

- Follow the following menu path: [Process](#) > [Raster](#) > [Extract...](#) . The [Select Objects](#) window appears.
- Navigate to the locations of the [SRFI](#) rasters that you plan to use as inputs to the [GRUVI.sml](#). For example, you probably would pick two rasters: [SRFIRL](#) and [SRFINA](#). If you plan to produce a set of [GRUVI](#) & [GRUBI](#) rasters for [more than one pair of input rasters](#), go ahead and select [all](#) of the [available SRFI rasters](#) for the scene being analyzed. When you confirm your selection (by clicking [OK](#)), the [Raster Extract](#) window appears.
- There are many tabs in the [Raster Extract](#) window. You need to examine each to ensure that all of the options are right for the present purpose. Do this in the following order:
 - [Rasters](#) tab: Should list the [SRFI](#) rasters that you selected for extraction. If not, [Exit](#) and re-select the rasters.
 - [Map Extents](#) tab: Don't change anything in this tab.
 - [Zoom/Orient](#) tab: Zoom Lines by 1.000 and Columns by: 1.000. Rotate: 0.00000 degrees. [Method: Nearest Neighbor](#). [Transfer Georeference](#): Enabled (pushed in).
 - [Values](#) tab: Output type: Same as input. Rescale: None. Null Value: Default.
 - [Insert](#) tab: All options disabled (not pushed in)
 - [Special](#) tab: Pyramid Output: Sample. Copy Metadata: Enabled. Default Raster Names: Polygon Name and Raster Name. Compression: Standard Lossless.
 - [Extract](#) tab: Change [Select](#): to [Range](#). When you do this, the [Raster Extract Object View](#) and [Raster Extract – Layer Manager](#) windows appear. The first raster on your extract list appears in the [View](#) window. Zoom into a part of the image that has a [vegetated](#) field that is obviously affected by background noise, e.g., a dark wet field. If you are unsure of whether or not the field is vegetated, you can add the [PVI](#) image to the Layer Manager and look for [PVI](#) values that are intermediate in value between [1000](#) and [2000](#). A [PVI](#) value of [1000](#) is for bare soil (no vegetation); you want a field that is partly vegetated.
 - The [Range](#) button is pushed in. You next need to pull out a [green box](#) with your mouse and reposition it over the wet field. Ideally, you want about half of the [green box](#) to be dry (light) and the other half to be wet (dark).

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- Try to avoid parts of the field where the vegetation density is highly variable; you want the main source of variability in the **green box** to be caused by variations in the brightness of the background materials (in this case, wet soils). You will see something like what is shown in [Figure E4A](#) below:

[Figure E4A. Raster Extract View Window after Selecting a Small Test Area for Extraction. Yuma, CO, SRFIRL Data, July 2, 2003.](#)



- When you are satisfied with the position of the **green box**, click the **Run...** button in the **Raster Extract** window. A **Select Objects** window appears.
- **Navigate** to the location of a new **Project File**. Name that file: **Test_Rasters** (.rvc). Name the rasters as **SRFIXT** and **SRFIYT** (if you have only two extracted rasters); alternatively, use the default names (if you have three or more extracted rasters).

You are now ready to run **GRUVI.sml**. See the **QUICK GUIDE** at the beginning of this tutorial to do this (using **GRUVI** parameters you have put in the **BLANK FORM**).

[E6. Is There an Example of the Use of GRUVI.sml for Non-Vegetation?](#)

Yes. But, this example will be given at the end of [FAQs by Jack F.pdf](#), which is the tutorial for [TASCAP.sml](#). This example will address the use of [GRUVI.sml](#) to produce a **GRUFI** raster that relates to open-water pixels in a **ASTER** image over **Stockton, CA** (May 9, 2001). **TC4** (designed to emphasize water) will be the "Y" raster and **TC3** (a collection of non-water materials) will be the "X" raster.

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